

Optimization of Electric Power Distribution in Ilorin Metropolis

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ABSTRACT

Electricity supply to the people in Ilorin has been faced with a lot of inadequacies and often met with several complains by the consumers (IBEDC 2016). This research optimized the efficiency level of Ibadan Electricity Distribution Company (IBEDC) in Ilorin using Linear Programming approach. Newton Gregory Interpolation Method was used to develop an efficiency distribution model. MATLAB and MAPLE were used for numerical computation of results. The findings revealed that IBEDC in Ilorin, has not been functioning to the best of their capacity. The study was able to predict future efficiency levels for the next five years (2022-2026) in the following order 72.16%, 75.84%, 80.22%, 93.43% and 93.43%. Based on this work, it is recommended that IBEDC in Ilorin need to ensure effective distribution of energy received from the Generating Companies (GENCOS), devoid of unnecessary lost. Government and policy makers are also advised to engage in an effective, verifiable and accountable investment towards ensuring allocated resources geared towards boosting power generation are judiciously used for targeted purposes to ensure and measure the growth in the power sector with time.

Keywords: Electricity, Linear Programming, Power Distribution, Optimization.

I. INTRODUCTION

The significance of electricity or steady power supply in any modern society today cannot be over emphasized because it is the most versatile form of energy which plays a very important role in the social and economic prosperity (Adekoya and Jeremiah 2019, Addeh 2021). Nwokoye et al (2017) Submitted that electricity is one of the most important blessings that science has given to mankind. It is important to our civilization, security, job creation and other aspects like health care systems (Simon 2021). It is often converted easily to numerous forms of energy for example lighting, heating, cooling, refrigeration and for operating appliances, computers, electronics, machinery, and other public transportation systems (Bhalla et al 2003). Olatunji et al (2018) observed that electricity is normally generated from conventional energy sources like fossil fuels (natural gas, coal), water power (hydro and pumped storage), biotic, fission etc., or non-conventional (renewable) energy sources like solar, wind, water power (tidal and waves), biofuels (biomass and biogas), geothermal, ocean thermal, or combination of both sources.

In Nigeria, a better part of her electricity is generated largely from natural or primary conventional energy sources like fossil fuels (gas), hydro power, which is unfortunately, grossly inadequate (Adenikinju 2005). Presently, the total electricity output in Nigeria is below 5,000MW despite having the capacity to generate up to 12,000MW which is insufficient for a rustic of over 195 million people that require about 40,000MW or more to sustain the essential needs of the population (Tena 2021). The electricity sector in Nigeria, as the biggest economy in Africa generates, transmits and distribute megawatts of electrical power that is significantly less than what is needed to meet basic household and industrial needs (Oladipo 2018). South Africa, the second largest economy with a 60 million population is generating 58,000 Megawatts. Egypt, the third largest economy with a 100 million population is generating 55,000 Megawatts (USAID 2021). The amount of electrical power generated usually fall as low as 1,750MW as a result of electricity theft from unauthorized connections, power loss in transmission, vandalism of kit, lack of proper maintenance of transformer, poor management and corruption among others are some of the reasons for sub-optimal production of electricity in Nigeria (Okpare and Okreghe 2020)

II. POWER DISTRIBUTION IN KWARA STATE

Kwara is a state in the Middle Belt region of the Federal Republic of Nigeria, bordered to the east by Kogi State, to the north by Niger State, and to the south by Ekiti, Osun and Oyo States, while its western border makes up part of the international border with Benin Republic (IBEDC 2016). Kwara has three Senatorial District, Kwara North, South and Kwara Central. Ilorin, the state capital of Kwara State has 20 political wards which comprise three Local Government Areas, Ilorin East, Ilorin West and Ilorin South with a total population of about 1 million people (IBEDC 2016). The Kwara region of Ibadan Electricity Distribution Company (IBEDC) comprising Challenge district, Omu- Aran, Jebba, Baboko, parts of Ekiti, parts of Kogi, parts of Oshogbo and Niger with total distribution output not more than 131.4 megawatts, is said to require at least 270 megawatts of electricity to ensure 24 hours power supply in Ilorin, the Kwara State capital, and its environs, according to (IBEDC 2016). The company had struggled over the years to deliver efficient electricity supply to both individual and industrial customers known as Maximum Demand customers (MDs) and Non-Maximum Demand customers (Non-MDs) in the city but due to certain constraints the electricity distribution has not been able to meet the efficient demand of the entire population in Ilorin metropolis (Tena 2021) Poor power supply situation in Ilorin could easily be blamed on: Inadequate generation of power supply to the state, power loss, energy theft, household energy consumption pattern and occasional system failures (Ejor 2021). According to Vanguard News published on the 18th March 2019, thirty communities in Ilorin, Kwara State capital on one Monday morning staged a peaceful protest over total blackout being experienced in the affected communities over the last six months. They said the last time they were supplied power by IBEDC, in the affected communities was on November 20, 2018. The affected communities are Alore, Oloje, Ita-Merin, Banni, Abayawo, Gunniyan, Anifowose, Pakata, Alfa-Yahaya, Oke-Agodi, Agbarigidoma, Gaa Oke-Idi emi, Ogidi, Temidire, Others are Abemi, Adeta, Aiyekale, Ifesowapo, Sakele, Olomoda, Albarika, Iberuoluwa, Ajegunle, Gaa-Osibi, Ifedayo, among others (IBEDC 2016).

III. MATERIALS AND METHODS

3.1. Data Description

This study utilized data set collected from IBEDC Unit of Ilorin Metropolis, Kwara State Nigeria. The data contained a record of the total amount of energy received and energy billed on a monthly basis from January 2015 to December 2021. It also included the billing details of various districts in Ilorin Metropolis. MATLAB and MAPLE were used for numerical computation of results.

3.2. Research Methodology

3.2.1. Linear Programming Method

The general linear programming problem is of the form:

$$\text{Optimize } Z = c_1x_1 + c_2x_2 + c_3x_3 + \dots + c_nx_n \text{ (Objective function)}$$

$$\text{subject to } a_{11}x_1 + a_{12}x_2 + a_{13}x_3 + \dots + a_{1n}x_n * b_1$$

$$a_{21}x_1 + a_{22}x_2 + a_{23}x_3 + \dots + a_{2n}x_n * b_2$$

$$a_{31}x_1 + a_{32}x_2 + a_{33}x_3 + \dots + a_{3n}x_n * b_3$$

$$\vdots$$

$$a_{m1}x_1 + a_{m2}x_2 + a_{m3}x_3 + \dots + a_{mn}x_n * b_m \quad (3.1)$$

$$\text{where } x_1, x_2, x_3 \dots x_n \geq 0$$

and * means <, >, ≤, ≥ or = sign

Note: In this research work, we denote all the parameters in the general formula as follows

c_i = Energy billed for the years under review

x_i =Efficiency in power distributed for the years under review

a_{ij} = Energy billed for the months in the years under review

b_{ij} = Energy received for the month in the years under review

			ININCOMING VARIABLES									
OUTGOING VARIABLES	BV	CB	x_1	x_1	x_1	...	x_n	x_{n+1}	x_{n+2}	...	x_{n+m}	x_B
	x_{n+1}	0	a_{11}	a_{12}	a_{13}	...	a_{1n}	0	0	...	0	⋮
	x_{n+2}	0	a_{21}	a_{22}	a_{23}	...	a_{2n}	0	0	...	0	⋮
	x_{n+3}	0	a_{31}	a_{32}	a_{33}	...	a_{3n}	0	0	...	0	⋮
	⋮											
		z_j	0	0	0							
	c_j	c_1	c_2	c_3								
	δ_j	$= z_j - c_j$										

Table 3.1: General Simplex Table. Source [6]

3.2.2. Newton Gregory Forward Difference Interpolation Method

Suppose the function $y = f(x)$ is known at $(n + 1)$ equispaced points x, x_1, \dots, x_n and they are y_0, y_1, \dots, y_n respectively i.e., $y_i = f(x_i), i = 0, 1, \dots, n$. Let $x_i = x_0 + i_h$ and $u = \frac{x-x_0}{h}$ where h is the step length [5].

The Newton Gregory Forward Interpolation formula is

$$y = f(x) = y_0 + u\Delta y_0 + \frac{u(u-1)}{2!}\Delta^2 y_0 + \dots + \frac{u(u-1)\dots(u-n+1)}{n!}\Delta^n y_0 \quad (3.2)$$

3.2.3 Newton Gregory Backward Difference Interpolation Method

This formula is useful when the value of $f(x)$ is required near the end of the table. h is called the step length of the difference and $u = \frac{(x-an)}{h}$, $f(a + nh - uh) = f(a + nh) + u\nabla f(a + nh) + \frac{u(u+1)}{2}!\Delta^2 f(a + nh) + \dots + \frac{(u(u+1)\dots(u+n-1))}{n}!\Delta^n f(a + nh)$ (3.3)

Difference Table

As before, suppose that we have a set of values of an unknown function $y_1, y_2, y_3, \dots, y_n$

corresponding to a set of valves of the (known) independent variable $x_1, x_2, x_3, \dots, y_n$

where $x_1 < x_2 < x_3, \dots < x_n$ To obtain the value of y corresponding to any x (where $x_1 < x_2 < x_3, \dots < x_n$) will be based on the values of the $n + 1$ data entries. Hence, $y_{r+1} - y_r$ is called the first difference of y_r denoted by Δy_r : $\Delta y_r = y_{r+1} - y_r$. Similarly, $\Delta y_{r+1} - \Delta y_r$ is the second difference: $\Delta^2 y_r = y_{r+1} - \Delta y_r$ For example, $\Delta^2 y_0 = \Delta y_1 - \Delta y_0 = (y_2 - y_1) - (y_1 - y_0) = y_2 - 2y_1 + y_0$. Similarly, $\Delta^2 y_1 = \Delta y_2 - \Delta y_1 = (y_3 - y_2) - (y_2 - y_1) = y_3 - 2y_2 + y_1$. In general term $\Delta^2 y_r = y_{r+2} - 2y_{r+1} + y_1$ $r = 0, 1, 2, \dots n - 2$.

$$\text{The third difference: } \Delta^3 y_r = y_{r+3} - 3y_{r+2} + 3y_{r+1}y_r \quad r = 0,1,2, \dots n - 3$$

Clearly, successive differences can be calculated and put into a table such as shown below

x	y	Δ_y	Δ^2_y	Δ^3_y	Δ^4_y	Δ^5_y
x_0	y_0	Δ_{y_0}				
			$\Delta^2_{y_0}$			
$x_1 (= x_0 + h)$	y_1	Δ_{y_1}		$\Delta^3_{y_0}$		
					$\Delta^4_{y_0}$	
$x_2 (= x_0 + 2h)$	y_2	Δ_{y_2}				$\Delta^5_{y_0}$
					$\Delta^4_{y_1}$	
$x_3 (= x_0 + 3h)$	y_3	Δ_{y_3}		$\Delta^3_{y_2}$		
			$\Delta^2_{y_3}$			
$x_4 (= x_0 + 4h)$	y_4	Δ_{y_4}				
$x_5 (= x_0 + 5h)$	y_5					

Table 3.2: General Forward Difference Table. Source [5].

IV. RESULTS AND DISCUSSIONS

In this section, the results of our findings are presented.

From the raw data collected from IBEDC unit Ilorin for the years under review it was observed that the amount of energy that is being distributed on a monthly basis is usually lesser than the amount of total energy received.

TOTAL ENERGY RECEIVED: 1548.2266

TOTAL ENERGY BILLED: 1179.32025

The efficiency in Power distribution was calculated using the formula:

$$ED = \frac{E_B}{E_R} \times 100 \tag{4.1}$$

Where

E_D is efficiency of distribution

E_B is energy billed

E_R is energy received.

MATLAB was employed for the optimization process, with MAPLE used for estimation of the forward and backward difference interpolations.

YEAR/MO NTH	JAN	FEB	MAR	APR	MAY	JUN	JUL	AUG	SEPT	OCT	NOV	DEC
2015	78.85 24	94.41 32	94.96 21	91.83 77	90.58 24	90.58 24	75.62 61	88.27 95	91.99 91	95.29 61	92.58 16	97.07 61
2016	86.75 26	80.70 16	86.24 81	89.87 76	93.07 58	91.35 63	95.00 34	95.27 29	90.88 87	88.92 36	94.95 26	9.517 8
2017	74.39.	93.43	76.46	74.87	83.52	56.87	68.94	76.94	80.81	67.63	60.93	60.16

	54	43	39	06	64	54	15	50	25	89	75	42
2018	89.93 93	82.65 91	67.92 24	66.65 25	66.07 91	60.09 84	81.21 68	75.58 64	53.23 52	49.90 26	81.21 68	63.99 91
2019	81.08 61	80.88 13	80.97 89	80.97 89	81.61 04	81.00 38	81.22 67	80.77 94	80.72 71	80.53 03	82.16 50	81.01 66
2020	81.42 81	81.45 63	79.66 17	79.66 16	48.40 61	49.64 13	56.12 69	54.98 73	55.55 56	58.77 15	66.58 65	64.61 39
2021	64.91 46	66.10 39	76.46 39	76.46 39	75.24 45	62.83 82	65.29 09	56.96 76	57.34 22	68.27 70	57.51 57	60.36 09

Table 4.1: Efficiency in Power Distribution Table

AVERAGE EFFICIENCY (%)	
2015	90.17
2016	90.31
2017	72.92
2018	69.88
2019	81.08
2020	64.74
2021	65.65

Table 4.2: Average Efficiency in Power distribution in Ilorin

YEAR/MO NTH	JAN	FEB	MAR	APR	MAY	JUN	JUL	AUG	SEPT	OCT	NOV	DEC
2015	3.481 6	1.018 24	0.842 98	1.334 33	2.195 97	1.642 36	4.335 29	2.188 84	1.370 04	0.872 29	1.270 29	0.504 61
2016	2.365 97	3.465 97	2.733 25	1.912 49	1.291 06	1.704 33	0.980 4	0.856 59	1.594 58	2.037 13	1.008 61	1.780 51
2017	4.639 72	1.130 9	3.587 4	4.600 63	3.191 91	7.895 15	4.842 54	3.594 66	3.802 04	6.129 8	8.371 32	8.272 76
2018	1.993 55	3.367 86	5.315 43	6.251 2	6.146 68	8.085 44	3.733 25	4.210 81	8.118 14	9.391 06	3.733 25	6.748 59
2019	3.581 6	3.500 24	3.372 98	3.404 33	3.265 87	3.470 46	3.462 49	3.684 84	3.761 4	3.305 29	3..178 49	3.761 61
2020	3.035 24	3.643 14	4.121 24	9.252 6	9.849 966	9.780 40	8.114 65	8.156 59	8.000 0	6.237 17	6.008 61	6.570 51
2021	7.286 24	6.567 69	3.587 4	4.600 63	4.297 42	6.157 92	4.852 87	8.501 92	8.196 47	5.480 87	9.229 08	8.576 06

Table 4.3: Unused Electricity Power in Ilorin

AVERAGE UNUSED POWER (%)	
2015	1.76

2016	1.81
2017	5.01
2018	5.60
2019	3.48
2020	6.91
2021	6.44

Table 4.4: Average Unused Power in Ilorin

From table 4.1 and table 4.3 the Linear Programming Problem is formulated as follows:

$$Max Z = 188.9259x_1 + 203.5588x_2 + 159.7029x_3 + 157.7134x_4 + 180.4172x_5 + 143.0604x_6 + 143.6087x_7 \quad (4.1)$$

Subject to:

$$13.35462x_1 + 15.39392x_2 + 13.48093x_3 + 17.82168x_4 + 15.35462x_5 + 16.18402x_6 + 13.48093x_7 \leq 132.3108 \quad (4.2)$$

$$17.20766x_1 + 4.49392x_2 + 16.14219x_3 + 16.05362x_4 + 14.80766x_5 + 16.00306x_6 + 12.80824x_7 \leq 130.2146 \quad (4.3)$$

$$15.88982x_1 + 17.14219x_2 + 11.65469x_3 + 11.25512x_4 + 14.3535982x_5 + 16.14219x_6 + 11.65469x_7 \leq 121.6592 \quad (4.4)$$

$$15.01319x_1 + 16.98123x_2 + 13.70715x_3 + 12.49441x_4 + 16.01319x_5 + 12.17799x_6 + 13.70715x_7 \leq 131.4505 \quad (4.5)$$

$$15.49392x_1 + 17.35455x_2 + 16.1818402x_3 + 11.97397x_4 + 14.49392x_5 + 9.241354x_6 + 13.06217x_7 \leq 128.0428 \quad (4.6)$$

$$15.79683x_1 + 18.01319x_2 + 10.41263x_3 + 12.17799x_4 + 14.79873x_5 + 9.641097x_6 + 10.41263x_7 \leq 129.9891 \quad (4.7)$$

$$15.45123x_1 + 18.64108x_2 + 10.74914x_3 + 16.14219x_4 + 14.98123x_5 + 10.38106x_6 + 9.128671x_7 \leq 123.8748 \quad (4.8)$$

$$16.48648x_1 + 17.2640x_2 + 11.99702x_3 + 13.05927x_4 + 15.48648x_5 + 9.96405x_6 + 11.25512x_7 \leq 126.7139 \quad (4.9)$$

$$15.75350x_1 + 15.84914x_2 + 16.01319x_3 + 19.2413x_4 + 15.75350x_5 + 74914x_6 + 10.74914x_7 \leq 128.0021 \quad (4.10)$$

$$17.67128x_1 + 16.35465x_2 + 12.80824x_3 + 9.354546x_4 + 13.67128x_5 + 9.354546x_6 + 11.79641x_7 \leq 124.4626 \quad (4.11)$$

$$15.83190x_1 + 18.97397x_2 + 13.05927x_3 + 16.14219x_4 + 14.64319x_5 + 11.97397x_6 + 12.49441x_7 \leq 135.9398 \quad (4.12)$$

$$16.75322x_1 + 16.99702x_2 + 12.49441x_3 + 11.99702x_4 + 16.05362x_5 + 11.99702x_6 + 13.05927x_7 \leq 135.5662 \quad (4.13)$$

Where

$x_1, x_2, x_3, x_4, x_5, x_6, x_7 \geq 0$ $x_i, i = 1(1)7$, denote the efficiency level of electricity distribution by the IBEDC Ilorin.

Adding the slack variables we have:

$$\text{Max } Z = 188.9259x_1 + 203.5588x_2 + 159.70291x_3 + 157.713x_4 + 180.4172x_5 + 143.0604x_6 + 143.6087x_7 \quad (4.14)$$

Subject to:

$$13.35462x_1 + 15.3939x_2 + 13.48093x_3 + 17.82168x_4 + 15.35462x_5 + 16.18402x_6 + 13.48093x_7 + x_8 = 132.3108 \quad (4.15)$$

$$17.20766x_1 + 4.49392x_2 + 16.14219x_3 + 16.05362x_4 + 14.80766x_5 + 16.00306x_6 + 12.80824x_7 + x_9 = 130.2146 \quad (4.16)$$

$$15.88982x_1 + 17.14219x_2 + 11.65469x_3 + 11.25512x_4 + 14.3535982x_5 + 16.14219x_6 + 11.65469x_7 + x_{10} = 121.6592 \quad (4.17)$$

$$15.01319x_1 + 16.98123x_2 + 13.70715x_3 + 12.49441x_4 + 16.01319x_5 + 12.17799x_6 + 13.70715x_7 + x_{11} = 131.4505 \quad (4.18)$$

$$15.49392x_1 + 17.35455x_2 + 16.1818402x_3 + 11.97397x_4 + 14.49392x_5 + 13.062x_6 - 7x_7 + x_{12} = 128.0428 \quad (4.19)$$

$$15.79683x_1 + 18.01319x_2 + 10.41263x_3 + 12.17799x_4 + 14.79873x_5 + 9.641097x_6 + 10.41263x_7 + x_{13} = 129.9891 \quad (4.20)$$

$$15.45123x_1 + 18.64108x_2 + 10.74914x_3 + 16.14219x_4 + 14.98123x_5 + 10.38106x_6 + 9.128671x_7 + x_{14} = 123.8748 \quad (4.21)$$

$$16.48648x_1 + 17.26406x_2 + 11.99702x_3 + 13.05927x_4 + 15.48648x_5 + 9.964057x_6 + 11.25512x_7 + x_{15} = 126.7139 \quad (4.22)$$

$$15.75350x_1 + 15.84914x_2 + 16.01319x_3 + 19.24135x_4 + 15.75350x_5 + 74914x_6 + 10.74914x_7 + x_{16} = 128.0021 \quad (4.23)$$

$$17.67128x_1 + 16.35465x_2 + 12.80824x_3 + 9.354546x_4 + 13.67128x_5 + 9.354546x_6 + 11.79641x_7 + x_{17} = 124.4626 \quad (4.24)$$

$$15.83190x_1 + 18.97397x_2 + 13.05927x_3 + 16.14219x_4 + 14.64319x_5 + 11.97397x_6 + 12.49441x_7 + x_{18} = 135.9398 \quad (4.25)$$

$$16.75322x_1 + 16.99702x_2 + 12.49441x_3 + 11.99702x_4 + 16.05362x_5 + 11.99702x_6 + 13.05927x_7 + x_{19} = 135.5662 \quad (4.26)$$

The slack variables are $x_8, x_9, x_{10}, x_{11}, x_{12}, x_{13}, x_{14}, x_{15}, x_{16}, x_{17}, x_{18}$, and $x_{19} \geq 0$.

The Objective function (Z) was derived from the sum of energy billed for the years under review (C_i) while the unknown variable (X_i) stands for the efficiency of the distribution. We have 12 unique constraints, which simply cover all months in a year for all the years under review. The constraints were formulated from energy billed and energy received for the months in the years under review.

B V	C B	x_1	x_2	x_3	x_4	x_5	x_6	x_7	x_8	x_9	x_{10}	x_{11}	x_{12}	x_{13}	x_{14}	x_{15}	x_{16}	x_{17}	x_{18}	x_{19}	XB	Rati o	
x_8	0	13.5 462	15.4 9392	13.4 8093	17.8 2168	15.3 5462	16.1 8402	13.4 8093	1	0	0	0	0	0	0	0	0	0	0	0	0	132. 3108	8.53 95
x_9	0	17.2 0766	4.49 392	16.1 4219	16.0 5362	14.8 0766	16.0 0306	12.8 0824	0	1	0	0	0	0	0	0	0	0	0	0	0	130. 2146	28.9 757
x_{10}	0	15.8 8982	17.1 4219	11.6 5469	11.2 5512	14.3 5982	16.1 4219	11.6 5469	0	0	1	0	0	0	0	0	0	0	0	0	0	121. 2146	7.09 71
x_{11}	0	15.0 1319	16.9 8123	13.7 0715	12.4 9441	16.0 1319	12.1 7799	13.7 0515	0	0	0	1	0	0	0	0	0	0	0	0	0	131. 4505	7.74 07
x_{12}	0	15.4 9392	17.3 5455	16.1 8402	11.9 7397	14.4 9392	9.24 1354	13.0 6207	0	0	0	0	1	0	0	0	0	0	0	0	0	128. 0428	7.37 81
x_{13}	0	15.7 9683	18.0 1319	10.4 1263	12.1 7799	14.7 9873	9.64 1079	10.4 1263	0	0	0	0	0	1	0	0	0	0	0	0	0	129. 9891	7.21 6
x_{14}	0	13.4 5123	18.6 4108	10.7 4914	16.1 4219	14.9 8123	10.3 8106	9.12 8671	0	0	0	0	0	0	1	0	0	0	0	0	0	123. 8748	6.64 53
x_{15}	0	16.4 8648	17.2 6406	11.9 9702	13.0 5127	15.4 8648	9.96 4057	&11. 2551 2	0	0	0	0	0	0	0	1	0	0	0	0	0	126. 7139	7.33 98
x_{16}	0	15.7 535	15.8 4914	16.0 1319	19.2 4135 4	15.7 535	10.0 0000	10.7 4914	0	0	0	0	0	0	0	0	1	0	0	0	0	128. 0021	8.07 63
x_{17}	0	17.6 7128	16.3 5465	12.8 0824	9.35 4546	13.6 7128	9.35 4546	11.7 9641	0	0	0	0	0	0	0	0	0	0	1	0	0	124. 4626	7.61 02
x_{18}	0	15.8 319	18.9 7397	13.0 5927	16.1 4219	14.6 4319	11.9 7397	12.4 9441	0	0	0	0	0	0	0	0	0	0	0	1	0	135. 9398	7.16 45
x_{19}	0	16.7 5322	15.9 9702	12.4 9441	11.9 9702	16.0 5362	11.9 9702	13.0 5927	0	0	0	0	0	0	0	0	0	0	0	0	1	135. 5662	7.97 59
	z_j	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
	c_j	188. 9259	203. 5588	159. 7029	157. 7134	180. 4172	143. 0604	143. 6087	0	0	0	0	0	0	0	0	0	0	0	0	0		
	$\delta_j = (z_j - c_j)$	- 188. 9259	- 203. 5588	- 159. 7029	- 157. 7134	- 180. 4172	- 143. 0604	- 143. 6087	0	0	0	0	0	0	0	0	0	0	0	0	0		

Table 4.5: Simplex Table

Hence, the efficiencies are

$$2015(x_1) = 0.298345760955721$$

$$2016(x_2) = 2.189705298436050$$

$$2017(x_3) = 0.951006449110309$$

$$2018(x_4) = 0.019508936363763$$

$$2019(x_5) = 4.066217803252357$$

$$2020(x_6) = -0.00000000016371$$

$$2021(x_7) = 0.831320172948608$$

Therefore,

$$Max Z = 1510.05467 \tag{4.27}$$

The indicated x-values represent the efficiency levels for the years under review from 2015 to 2021, which shows that, IBEDC in Ilorin can perform better than their current outputs. Their performance in 2016 and 2019 have the highest efficiency levels, one of the factors responsible for this was there were significantly lesser amount of unutilized power in those two years in comparison to the rest of the years in the study. The result however, indicated a low level of efficiency in the year 2020, due to an exorbitant rate of unutilized power in the year and some other logistics and management problems according to a report by the IBEDC Kwara Region on one of their social media handle on the 21st September, 2020 (IBEDC, 2020). We observed that the amount of energy that is being distributed on a monthly basis is usually lesser than the amount of total energy received by the distribution unit. The result shows that the maximum solution obtained (equation 4.27) is higher than the total amount of energy used from the available energy, that is total energy billed for the years under review by the IBEDC unit of Ilorin Metropolis. The difference is about (330.7344MW) which is enough to take care of at least another three years based on the capacity with which they are functioning presently.

Using Newton Gregory Backward difference interpolation formula we derived the prediction model from Table 4.2 by expanding the equation using MAPLE.

Hence, the prediction model is given as

$$y(x) = 0.1915555556x^6 - 5.091333334x^5 + 53.16680555x^4 - 275.248333x^3 + 731.4616389x^2 - 920.3478334x + 481.5100000 \tag{4.29}$$

Equation (4.29) is the prediction model of power distribution in Ilorin Metropolis.

Using the Newton Backward Difference Interpolation formula we derived the lost in electrical power model from Table 4.4. Hence, the model is given as

$$y(x) = 0.03995833333x^6 - 1.0563750000x^5 + 9.513541666x^4 - 42.03145833x^3 + 95.44650000x^2 - 105.0621667x + 49.59000000 \tag{4.30}$$

The Efficiency Model Curve of Power Distribution in Ilorin Metropolis

Power Distribution Efficiency

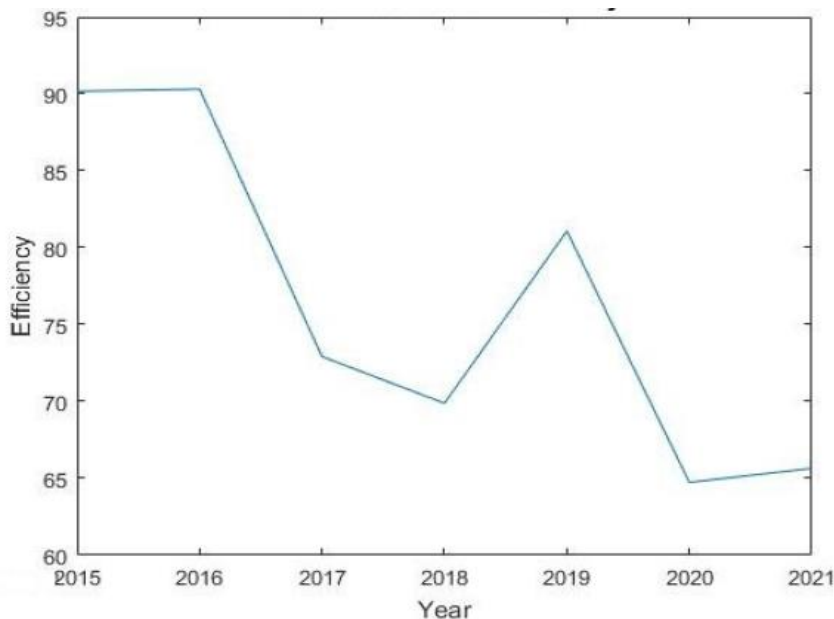


Figure 4.1: The efficiency model of Power Distribution in Ilorin

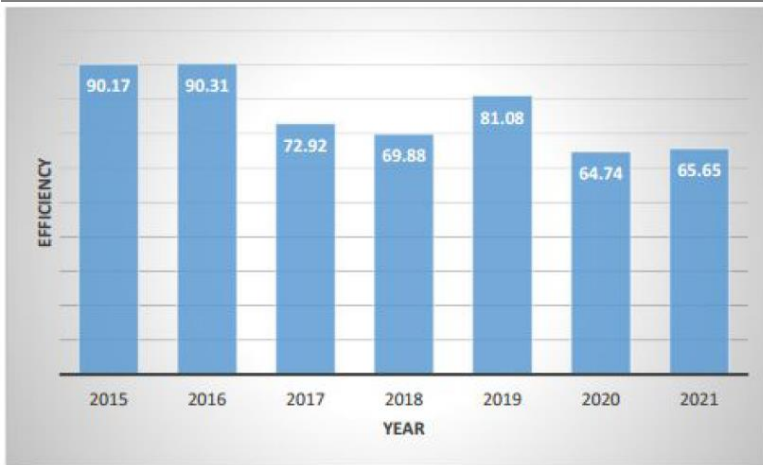


Figure 4.2: The Efficiency Chart of Power Distribution in Ilorin

From the curve in Figure 4.1 and chart in Figure 4.2 it was observed that between 2015 and 2019, the efficiency level was far above average based on the amount of energy received by IBEDC unit in Ilorin Metropolis and was judiciously distributed.

It was also observed that the efficiency level in year 2020 was the lowest due to a very high rate of unutilized power received by the distribution unit. Other factors that also influenced this include poor maintenance system, energy theft and loss in transmission as illustrated in Figure 4.3.

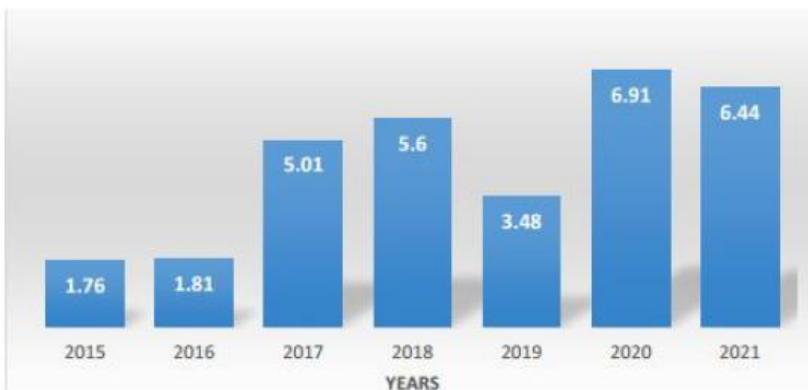


Figure 4.3: Lost in electrical power in Ilorin Metropolis

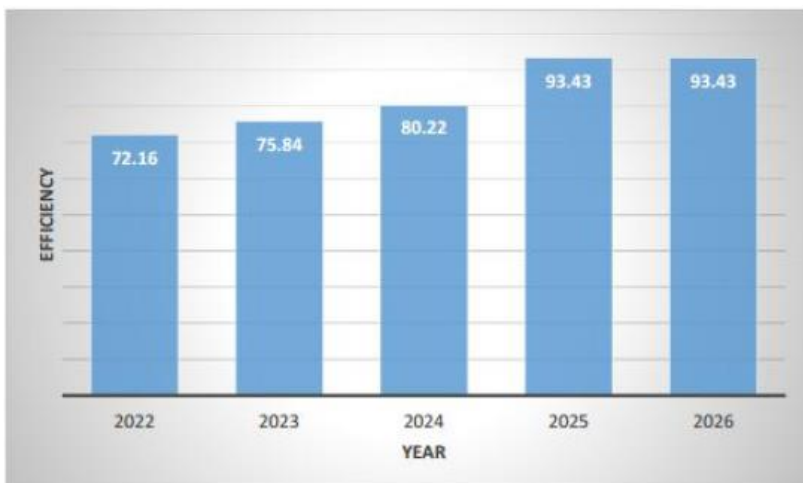


Figure 4.4: Efficiency prediction curve

The efficiency model (equation 4.28) was used to plot the efficiency curve in Figure 4.1 and the efficiency chart, Figure 4.2 and was also used for the prediction as illustrated in the Figure 4.4 It showed the gradual optimum values for the next five years to come based on the model of efficiency in power distribution in Ilorin.

V. CONCLUSION

This study investigated the efficiency level of power distribution in Ilorin using linear programming method of optimization technique. The result showed that IBEDC in Ilorin, despite receiving electric power that is not sufficient to serve the people of Ilorin effectively have not been functioning to their best based on the amount of power they are able to bill from the amount they are receiving currently. More so, the study also established that there is a significant loss of energy from the little available that can be distributed in order for the unit to function optimally for a better performance. The study was able to predict future efficiency levels for the next five years in the following order 72.16%, 75.84%, 80.22%, 93.43% and 93.43% using Matlab and Maple for numerical computation of the efficiency model created by Newton Gregory Backward Difference Formula. From this research work, it can be concluded that despite the huge investments in the power sector since after independence, the country with over 180 million people has a recurring cycle with little or no development in the power sector. Particularly in Ilorin Metropolis the capital city of Kwara state, the research was able to establish that the IBEDC in Ilorin has been receiving voltage of electric power that is very small compare to the amount needed to serve the entire city effectively. Obviously, it is a public knowledge that there is a problem of low power generation from the national grid which directly influences the little available amount that is being transmitted and distributed to various states and to local government level. The energy sector can however be improved to function optimally if we reduce the amount of wasted energy on a monthly basis and make judicious use of the little being generated till the system becomes better.

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